## **ECON 405**

## **Economic Growth and Development**

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Dr. Yetkiner

## Midterm

## (The Solow Model of Economic Growth)

- **1.** (50 Points) Suppose the production function of an economy is characterized by  $Y_t = K_t^{\alpha} \cdot L_t^{1-\alpha}$ , where  $L_t = e^{nt}$ .
- **a**. (**5 Points**) What is the intensive form of the production function?

**b.** (15 Points) Starting from the Fundamental Equation of Growth (FEG), find the steady-state level of  $k_t$ , given that  $\delta > 0$ , n > 0, and  $I_t = s \cdot Y_t$ .

c. (10 Points) Find consumption per worker at steady state,  $c_{ss}$ .

d. (10 Points) What is the "golden rule of capital accumulation" / "golden saving rate"?

**e**. (10 Points) Suppose s=0.24,  $\alpha=0.25$ ,  $\delta=0.04$ , and n=0.02. Find numerical values of  $k_{ss}$ ,  $y_{ss}$  and  $c_{ss}$ .

- **2.** (10 Points) Suppose that the production function is characterized by  $Y_t = A \cdot K_t^{1/3} \cdot L_t^{2/3}$ , where A = 3 is a technology parameter.
- **a**. (**5 Points**) Find  $MPP_K$ .
- **b**. (**5 Points**) Find *MPP*<sub>L</sub>.

3. (20 Points) Suppose that aggregate production function of an economy is characterized by  $Y_t = (K_t^{0.5} + L_t^{0.5})^2$ , where  $Y_t$  is output,  $K_t$  is capital,  $L_t$  is labor. Determine whether this production function satisfies Inada conditions.

**4.** (30 Points) Suppose that you are given a Solovian model in which the production function is characterized by  $Y_t = K_t^{\alpha} \cdot (A_t \cdot L_t)^{1-\alpha}$ , where  $L_t = L_0 e^{nt}$  and  $A_t = A_0 e^{xt}$ . Discuss in detail how this framework is used in **testing** differences in standards of living (level of economic development) across countries and income convergence. In short, discuss empirical use of the Solovian growth framework.